

IX. Three computer component assembly methods were compared by Insel Corporation. Employee efficiency was based upon production time and product quality.

A. Use ANOVA analysis to test at the .05 level of significance whether mean employee efficiency of these assembly methods are equal.

ANOVA Analysis of Assembly Methods						
Employee Efficiency Ratings for 3 Treatments (T)						Row Totals Required for Calculations
Method 1		Method 2		Method 3		
Score $X_1$	$X_1^2$	Score $X_2$	$X_2^2$	Score $X_3$	$X_3^2$	
4	16	6	36	8	64	
6	36	7	49	8	64	
7	49	4	16	9	81	
<u>7</u>	<u>49</u>	<u>7</u>	<u>49</u>	<u>9</u>	<u>81</u>	
$\sum X_T$	24	24		34		$\sum x = 82$
$(\sum X_T)^2$	576	576		1156		
$n$	4	4		4		$N = 12$
$\frac{(\sum X_T)^2}{n}$	144	144		289		$\sum [\frac{(\sum X_T)^2}{n}] = 577$
$\sum X_T^2$		150		290		$\sum x^2 = 590$

- $H_0 : \mu_1 = \mu_2 = \mu_3$   $H_1 : \mu_1 \neq \mu_2 \neq \mu_3$
- F is the test statistic and  $\alpha = .05$ .
- If F from the test statistic is beyond the critical value of F, the null hypothesis will be rejected.
- $df = t - 1 = 3 - 1 = 2$   
 $df = N - t = 12 - 3 = 9$   
f for .05 level of significance is 4.26.
- Apply the decision rule.

$$F = \frac{MS_T}{MS_E} = \frac{8.335}{1.44} = 5.79$$

Reject  $H_0$  because  $5.79 > 4.26$ .  
Training methods had different means.

$$SS_T = \sum \left[ \frac{(\sum x_T)^2}{n} \right] - \frac{(\sum X)^2}{N}$$

$$= 577 - \frac{82^2}{12}$$

$$= 16.67$$

$$MS_T = \frac{SS_T}{t-1} = \frac{16.67}{3-1} = 8.335$$

$$SS_E = \sum x^2 - \sum \left[ \frac{(\sum x_T)^2}{n} \right]$$

$$= 590 - 577$$

$$= 13.00$$

$$MS_E = \frac{SS_E}{N-t} = \frac{13}{12-3} = 1.44$$

$$SS_{TOTAL} = \sum x^2 - \frac{(\sum x)^2}{N} = 590 - 560.33 = 29.67$$

B. Determine at the .01 level of significance whether there is a difference in performance of those who received teaching methods (treatments) 1 and 3.

$$\bar{X}_1 = \frac{\sum x}{n_1} = \frac{24}{4} = 6.0$$

$$\bar{X}_3 = \frac{\sum x}{n_3} = \frac{34}{4} = 8.5$$

The t for  $\alpha/2$  and  $N - t$  degrees of freedom ( $12 - 3 = 9$ ) is 3.25.

$$(\bar{X}_1 - \bar{X}_3) \pm t \sqrt{MS_E \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}$$

$$(8.5 - 6.0) \pm 3.25 \sqrt{1.44 \left( \frac{1}{4} + \frac{1}{4} \right)}$$

$$2.5 \pm 2.758$$

$$-.258 \leftrightarrow 5.258$$

This range indicates the difference between these means could be zero.